

Construct  $R_{\mu\nu\rho\sigma}$  &  $R_{\mu\nu\rho\sigma}$ , which is  
non-zero everywhere (unlike  $R=0$ )  
We'll see  $R_{\mu\nu\rho\sigma}$  is finite  
at  $f=2GM$

Every other scalar is finite.

One can find explicit coordinate  
sys. such that in the new coordinate  
system the metric is finite.

→ in that system the scalars are manifestly  
finite - of course they are finite in  
any other coord. sys. - ~~only one~~  
~~coord. sys. where the singularity is not~~  
original)

(The choice of the above coord. is for a  
far-away observer)

The singular metric in the  
coordinate system of an asymptotic  
observer has interesting effects  
→ Make this into a black hole

[We'll see if we start from a pt.  $r < 2GM$   
& follow a time-like curve, we can never  
reach asymptotic ~~to~~ i.e., we can never come out  
of the black hole] - time-like geodesics are  
relevant because they give the  
trajectory of massive particles - null-curves  
also can't come out - only spacelike  
curves can come out]

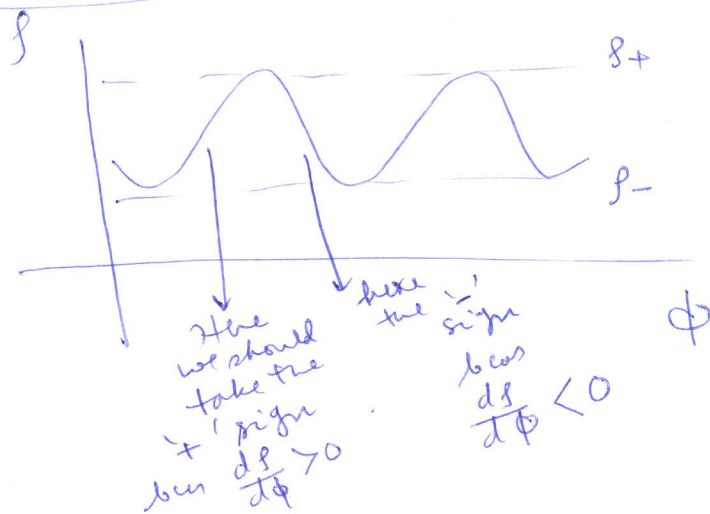
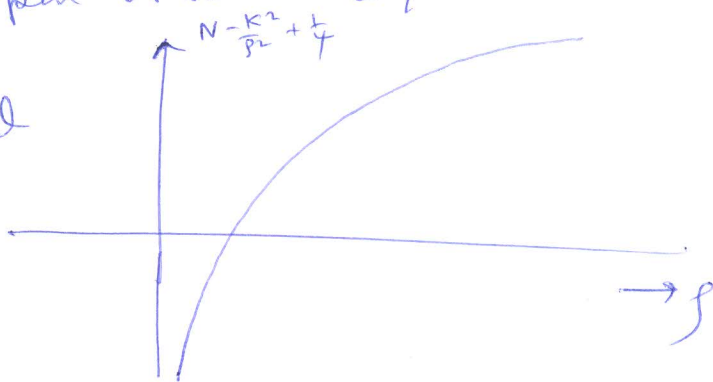
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$$\frac{d\phi}{ds} = \pm \frac{K \sqrt{\chi(s)}}{s^2} \frac{1}{\left(N - \frac{K^2}{s^2} + \frac{1}{4}\right)^{1/2}}$$

As  $s \rightarrow 0$ , the curve is -ve, so the curve must cross the  $s$ -axis at least once — for bound orbit it must cross  $s$ -axis twice.

For open orbit ~~circle~~ / Unbounded orbit  $\Rightarrow$

Whether it will be bound or unbound will be det. by  $N$  &  $K$



(We determine  $s_+$  /  $s_-$  by finding the zero(s) of  $N - \frac{K^2}{s^2} + \frac{1}{4} \Rightarrow$

$$N - \frac{K^2}{s_+^2} + \frac{1}{4} = 0$$

$$N - \frac{K^2}{s_-^2} + \frac{1}{4} = 0$$

We get  $N = \frac{1}{s_+^2 - s_-^2} \left\{ \frac{s_-^2}{\chi(s_-)} - \frac{s_+^2}{\chi(s_+)} \right\}$

